Wave-particle interactions in the outer radiation belts

O. V. Agapitov\(^1,2\), F. S. Mozer\(^1\), A. V. Artemyev\(^3\), D. Mourenas\(^4\), V. V. Krasnoeselkikh\(^5\)

\(^1\)Space Science Laboratory, the University of California 7 Gauss Way, Berkeley, CA 94720, USA
\(^2\)Taras Shevchenko National University of Kyiv, Gushkova av., 4, 03127, Kyiv, Ukraine
\(^3\)University of California Los Angeles, Los Angeles, CA, USA
\(^4\)CEA, DAM, DIF, Arpajon, France
\(^5\)LPC2E/CNRS-University of Orleans, France

Data from the Van Allen Probes have provided the first extensive evidence of non-linear (as opposed to quasi-linear) wave-particle interactions in space, with the associated rapid (a fraction of a bounce period) electron acceleration, to hundreds of keV by Landau resonance, in the parallel electric fields of time domain structures (TDS) and very oblique chorus waves. The experimental evidence, simulations, and theories of these processes are discussed.

**Key words:** radiation belts, wave-particle interaction, plasma waves and instabilities

Understanding the formation, dynamics, and loss of particles in the Earth's radiation belts is a problem that has been studied for decades, and that remains incomplete [33, 61, 62]. The Van Allen radiation belt particle populations exist in a dynamic equilibrium between losses (mainly due to particle precipitation to the upper atmosphere) and re-filling due to external injections, transport and acceleration processes [39]. The recent results from the Van Allen Probes support the local nature of particle acceleration [51, 54], and it is now generally agreed that in-situ local acceleration mechanisms are important to the outer radiation belt.

A favoured candidate for driving in-situ acceleration (and scattering) is the interaction between whistler waves and electrons [33, 61, 62]. Whistlers in the magnetosphere manifest themselves as electromagnetic perturbations generated near the geomagnetic equator and called chorus (structured, coherent, wave packets [66]) and hiss (diffusive, wide band emissions mostly with randomized phases [45, 63]). Chorus waves are the most intense natural VLF electromagnetic emissions in the magnetosphere. The maximum chorus wave amplitudes are located in the core of the outer Van Allen radiation belt [1]. This fact, as well as the closeness of their frequency to the electron cyclotron frequency, make them one of the key factors that control the dynamics of the outer radiation belt [33, 54, 61, 62].

Interactions between whistler waves and electrons are analyzed in two approximations:

1. The quasi-linear approach, where particles interact with large numbers of small amplitude waves having random phases, and the characteristic time scales are hours and days. The quasi-linear approach

to wave-particle interactions was developed in [35, 36, 64], and applied to the radiation belts in [40] with inclusion of diffusion in particle energy and pitch-angle space [2, 10, 18, 31, 32, 47, 57, 58, 59] and radial transport of electrons from the tail [38, 60]. For the moment, long time progresses and models of radiation belts dynamics are provided in a frame of this quasi-linear approximation [35, 61]. The averaged (~ 1s and more) spectral measurements of magnetic field perturbation with low resolution plasma density measurements (from Cluster, THEMIS, Van Allen Probes missions, see details below) are good enough to provide the experimental basis for such models [3, 18, 44, 49, 58]. The problems related to whistler generation and fast anisotropy relaxation of hot electrons population, however, remained out of scope of interests, and the results are mostly obtained from the numerical self-consistent calculations on the basis of Particle-In-Sell (PIC) models. These results indicate a large initial anisotropy of electron temperature (greater than 2 for non-thermal population, which has not been observed in averaged data) and its fast relaxation (during ~ 10 gyropериods) to values approximately less than 2 [28]. The recent results from Cluster mission showed that significant part of whistler waves in the outer radiation belts is oblique [1, 6, 7, 13]. These results were confirmed by numerical simulations based on ray tracing approximation [21, 23, 24, 26]. The presence of oblique waves sufficiently affects scattering processes decreasing life time of electrons of near relativistic and relativistic energies [11, 12, 13, 18, 46, 49]. The dependence of chorus wave obliqueness on the geomagnetic activity explains well the geomagnetic storm dynamics of the electron population in the

\^agapitov@ssl.berkeley.edu, agapitov@univ.kiev.ua

O. V. Agapitov, F. S. Mozer, A. V. Artemyev, D. Mourenas, V. V. Krasnoeselkikh, 2015
outer radiation belt [13, 14, 47]. Questions of generation of very oblique waves are considered in [48].

2. The non-linear approach where particles can be trapped into the effective potential of large amplitude coherent waves and the characteristic scales of interactions could be fraction of the bounce period or even a couple of gyroperiods. Discovery of large electric field amplitudes in whistler waves, above 100 mV/m [2, 25, 27, 34, 69] and numerous observations of large amplitude whistlers by Van Allen Probes, caused renewed interest in non-linear effects in wave-particle interactions. The interaction (electron acceleration) of electrons with coherent whistlers was studied as due to the non-linear cyclotron resonance of electrons moving in the opposite direction of a parallel whistler wave to satisfy the resonance condition [22, 53, 65] (the concept of such interaction is well established analytically and through the numerical simulation, however just several cases were established from the observations, see for example [51]). The temporal and spatial scales of chorus source and wave coherence are important parameters for feasibility of nonlinear interaction processes, were studied in [5, 9, 53]. The source region scale was found to be around 600 km at $L \sim 4.5$ from Cluster measurements and about 3000 km from measurements of five THEMIS spacecraft [9]. Numerous observations of similar chorus wave packets aboard Van Allen Probes spacecraft at separations greater than 500 km indicate that the chorus source spatial scales varies from 500 to 1000 km in the outer radiation belt [5]. Thus, recent results show that the scale of the source region for chorus waves is much greater than the wavelength ($\sim 10 - 20$ wavelengths) and that this scale may depend strongly on $L$-shell. The temporal whistler wave coherence is discussed in the recent paper [29], where the high level of time coherence was obtained for chorus waves (rising and falling tones) but a much lower coherence level was obtained for hiss. The detailed study of nonlinear trapping and acceleration as well as of breaking the resonance conditions for cyclotron and Landau resonances is presented in [17].

It was shown that the majority of the observed large amplitude waves were very oblique [2, 25] and thus had large electric field, also, aligned to the background magnetic field (see Figure 4 in [2]). Large electric field component parallel to the background magnetic field allows these waves to interact with electrons through the Landau resonance that reduces the energy threshold for non-linear trapping to $\sim 1$ keV [2, 16]. This interaction provides acceleration along the background magnetic field line, which can cause precipitation of $10 - 100$ keV electrons [16] that presumably becomes the source for X-ray micro-bursts. Moreover, such interaction provides the significant feedback for wave fields and tends to the nonlinear transformation of waveforms that was demonstrated on the basis of electric field measurements on board the Van Allen Probes [51] making the dramatic changes for distributing function on time scales about a couple of gyroperiods, due to trapping. The Landau trapping responsible for such interactions needs high resolution particles data for confirmation (all results were obtained from the numerical PIC simulation [28]) and these processes are the subject for future projects. The Landau resonance trapping can provide the feedback response from trapped particle to the wave fields and Van Allen Probes project presents the high quality data for electromagnetic fields and particles to study in details these nonlinear effects.

Data from the Van Allen Probes have provided the first extensive evidence of nonlinear (as opposed to quasi-linear) wave-particle interactions in space with the associated rapid (about a bounce period) electron acceleration to tens (and hundreds in some cases) of keV by the Landau resonance in the parallel electric fields of time domain structures (TDS) [15, 51, 67] and very oblique chorus waves [4]. The Van Allen Probes A and B were launched on August 30, 2012, aiming at studying the radiation belts with unprecedented detail [43]. The data is provided by the following instruments on board the Van Allen Probes: the Electric Field and Waves (EFW) instrument [70] for electric field waveforms, the Electric and Magnetic Field Instrument Suite and Integrated Science (EMFISIS) [37] for electric and magnetic spectral and polarization information, the DC magnetic field data and electron cyclotron frequency $f_{ce}$, the electron plasma frequency value $f_{pe}$ (deduced from the upper hybrid frequency); the Energetic Particle, Composition, and Thermal Plasma (ECT) instrument [56] data of the Helium Oxygen Proton Electron (HOPE) detector for electron fluxes below 50 keV [30], and the Magnetic Electron Ion Spectrometer (MagEIS) 30 keV to 4 MeV measurements [20]. The waveform data was transmitted at 16,384 samples/s (35,000 from EMFISIS) for 5 s continuous intervals in the burst mode (triggered automatically by large amplitude signals), as well as continuously every 6 s under the form of full spectral matrices for 65 frequencies (logarithmically spaced from 3 Hz to 16 kHz for EMFISIS).

Figure 1 provides an example of these nonlinear processes. Panels (a) and (b) give the spectra of the magnetic and electric field during a 20 minute interval. The red horizontal line in each of these panels gives the electron gyrofrequency and the white line below it is half this frequency. Thus, the waves seen at 300 – 1000 Hz are lower band chorus. Panel (c) gives the flux ratio, defined as the average of the electron number flux at the two lowest and two highest peak angles divided by the 90 degree flux. Flux ratios of 2 – 4 (field-aligned flux two or four times greater than the 90 degree flux) are observed for $\sim 1$ keV electrons between about 1120 and 1126 UT, while chorus waves were measured by the wave de-
ectors. Panels (e), (f), and (g) give the three components of the magnetic field in field-aligned coordinates while panels (h), (i), and (j) give the same information for the electric field. The parallel components of the magnetic and electric fields are in panels (g) and (j), respectively. In panel (j), it is seen that the parallel electric field is distorted to produce periodic pulses of parallel electric field that are viewed in the expanded plot of panel (k). Panels (l) and (m) give the electron pitch angle distributions before and during the time of the non-linearity. They show that the 100 eV to 3 keV electrons (the green and yellow curves) became field-aligned as a result of this non-linear interaction. Thus, this figure provides an example of the non-linear interaction between a chorus wave and the electron distribution that results in a distorted parallel electric field (panel j) and field-aligned acceleration of keV electrons by this distorted field (panel m).

Formation of TDS from the background fields and plasmas is discussed in [8, 28, 68]. TDS structures are observed on the night side at L values of ~5 during perturbed conditions in the magnetosphere. They coincide with magnetic energy injections and field-aligned currents and, sometimes, with injected particles, although injected particles may not frequently penetrate to these L-shells. A statistical analysis will be performed to determine if a correlation between field-aligned currents and TDS exists in the Van Allen Probe measurements. During the event reported in [51] and [8], whistler waves and TDS structures were simultaneously present. Moreover, more detailed analyses have shown that these two types of structures can be phase correlated. This suggests that some TDS structures can be directly generated by wave-wave (as it was shown in [8]) and/or wave-particle interactions with whistlers and preliminary simulations support such a hypothesis. Nonlinear whistler wave-wave and wave-particle interactions will be studied to determine the role of these waves in the generation and evolution of TDS and modification of the particle distributions. TDS generation may be related to the large amplitude whistler waves that are frequently observed in the outer radiation belt [2]. Preliminary studies have shown that such whistlers are mainly very oblique with a significant parallel electric field component. This field can trap and accelerate electrons (see [16, 19] for details) and it can produce nonlinear effects on the wave [34, 51]. Such non-linear steepening of whistlers can further manifest itself in growth of upper wave harmonics and strong localization in space with a consequent increase of the parallel electric field perturbation. The statistics of large amplitude whistler waves with the statistics of different types of TDS will be generated. PIC simulations [28] suggested that the parallel electric fields of off-angle whistlers trigger the formation of intense bipolar electric field structures and double layers.

An example of TDS and parallel electron acceleration is given in Figure 2 from Van Allen Probe B measurements on 2012 – 11 – 01 (panels are similar to those in Figure 1). Field-aligned electrons with energies as high as hundreds of eV are seen in the flux ratio plot of panel (c), while TDS, identified by the broadband electrostatic noise, are observed in panel (b). The free energy source for the TDS and the field-aligned electrons might be the field-aligned current and injections - such current systems are often observed together with TDS [41, 42]. Examples of pitch angle distributions before and during a TDS event are presented in panels (h) and (i), showing the field-alignment of 500–5000 eV electrons. It is noted, that the injected electrons did not have field-aligned distributions, which is evidence that such distributions were made by the TDS. The parallel electric field of the TDS is shown in panel (f) (second plot from the bottom of the central figure) and the parallel magnetic field is given in panel (e) (third panel from the top of the central figure). The fine structure of the single TDS is shown in panel (g). These plots show that the observed TDS are the electrostatic double layers with amplitudes of ~30 mV/m in the parallel electric field component. TDS velocity is estimated to be about 3000 km/s. Statistics of TDS distribution in the outer radiation belts and association with other phenomena of geomagnetic activity can be found in [41, 42].

The role of TDS in the acceleration of thermal electrons is discussed in [15, 67]. The interaction of TDS with thermal electrons ([15] and [51]) causes parallel electron acceleration to keV energies. This is important for developing the seed population required for further relativistic acceleration, and TDS may thus be important for the dynamics of the radiation belts. To test whether TDS provide this seed population, a systematic approach is planned, based on statistics. The objective is to compare examples of the effect on thermal electrons of whistlers with TDS, whistlers without TDS and TDS without whistlers. Such data will depend on time domain waveforms collected and transmitted to the ground. Time domain data are required because power spectra alone do not provide sufficient information on the obliqueness of the whistlers, nor on the type of TDS. For example, a low frequency signal in the power spectrum could be due to TDS, or to lower hybrid waves, or to neither; therefore, time domain data is required.

High-time resolution measurements, such as those presented in Figure 1 and 2, have thus far been analyzed during ~5 second bursts at a duty cycle of about 1% of the time from both the Van Allen Probes and THEMIS. While this data provides a peek into the relevant processes, it is planned to obtain a microscopic view of the physics by analyzing hours of continuous high time resolution plasma and field data from the Van Allen Probes during night-time
apogees in 2014 through 2015 and from THEMIS during dedicated high data rate bursts of tens of minutes each in 2015 and 2016. Many of these burst collections will be done in conjunction with the Canadian ground based array of auroral images in order to study the physics that leads to particle precipitation and auroras. The apogee of the Van Allen probes passed through dawn and to 2200 MLT by late summer of 2015. During this time interval, the apogee passed through the in-situ local acceleration region near midnight, which is the locale of the largest TDS concentration. The electric field instrument operated in the new mode in which continuous measurements at a sample rate of 16384 samples/second for 3 – 5 hour intervals were made to supplement the 5 second bursts. Similarly, during 2014 – 2015, tens of examples of minute burst of plasma and field data were collected on THEMIS at times of conjunctions between the satellite and one or more Canadian ground stations. Accordingly, a systematic approach will be performed in which the high-time resolution observations gathered by the Van Allen Probes and THEMIS will be subjected to theoretical interpretation, modeling, and computer simulation.

The model of TDS interactions with thermal electrons has been developed in [15, 67] and the results reproduce the main features of particle dynamics obtained from the Van Allen Probe measurements (Figures 1 and 2). The multiple interactions with TDS affect mostly particles below 1 keV but trapping effects can accelerate electrons to 10 – 20 keV.

The influence of TDS in relativistic electron acceleration and scattering is studied in [50, 51]. Low energy electrons can be accelerated to relativistic energies by the two-step process of keV acceleration by a small number of resonant interactions with TDS [15] followed by whistler cyclotron resonance acceleration, as was shown experimentally and by a test particle simulation in [51]. A multi-case study of this two-step process will be carried out through a statistical analysis of electron distribution function, TDS, and chorus wave parameters in TDS and whistler events in order to determine the key factors controlling these dynamics. An important issue is the role of upper band whistlers because the cyclotron resonance condition is satisfied by lower energy electrons as the wave frequency approaches the electron cyclotron frequency. Upper band waves (with frequencies from 0.55 to 0.8 of the local electron gyrofrequency) are generally assumed to be less intense than lower band chorus whistlers (with frequencies from 0.1 to ~ 0.45 of the local electron gyrofrequency) but statistical studies of upper band chorus have been limited by instrumental frequency responses (~ 4kHz on Cluster and THEMIS). One of the proposed tasks will be the detailed study of upper band whistlers to consider their occurrence frequency and role in particle acceleration (on the Van Allen Probes the high rate time domain data has a frequency response to 8kHz.). Not considered in the two-step process of relativistic electron acceleration is the possibility of additional acceleration by the Landau resonance with oblique whistlers [16]. This mechanism requires a low threshold in electron energy (~ 2 – 10keV) to satisfy the trapping conditions and it can function efficiently to accelerate (up to 100keV) and scatter electrons after their pre-acceleration by TDS.

Observations by the Van Allen Probes have revealed nonlinear features of the ELF/VLF waves in the outer radiation belt that can be important for particle diffusion and acceleration. A brief review of recent publications dedicated to nonlinear wave-particles interactions is presented here. In conclusion, it has been shown that during local night time at L ~ 5, multiple electric field bursts of short duration (several hundred micro-seconds) and large amplitudes (up to 300 nV/m), called time domain structures (TDS) [50, 52], are observed [15, 51] to correlate with energetic particles having magnetic-field-aligned pitch angle distributions. Such TDS can provide the first step [15, 67] in a two-step process that accelerates thermal electrons to relativistic energies [51]. The second step in the process is perpendicular acceleration by cyclotron resonance with whistlers. Thermal particles cannot be accelerated by such chorus waves because they do not satisfy the resonance condition (see Section 1.2 for details). Injected particles may not penetrate to the required depth for them to become a significant source of seed particles for the cyclotron [51] and/or the Landau resonance [16]. Because TDS acceleration leads to an increase of the electron parallel velocity (see figure 3 in [15]) and because the whistler resonance threshold depends on this parallel velocity, the TDS interaction makes it possible for thermal electrons to be accelerated to relativistic energies through the chain of trapping [51]. The simultaneous observations of whistler waves and TDS along with relativistic accelerated electrons provide clear evidence that this two-step process is active. Additional evidence is that TDS are observed to accelerate electrons to keV energies in the absence of whistlers and that whistlers alone do not accelerate electrons. These facts imply that two steps are crucial for acceleration of electrons from thermal to relativistic energies.

ACKNOWLEDGEMENT

The work by O.A. was performed under JHU/APL Contract No. 922613 (RBSP-EFW).

REFERENCES

Advances in Astronomy and Space Physics


[60] Schulz M. & Lancerotti L. J. 1974, Particle diffusion in the radiation belts
[64] Trakhtengerts V. Y. 1966, Geomagnetism and Aeronomy, 6, 827
Fig. 1: Observations of nonlinear whistler waves on Van Allen Probe B spacecraft on May 1, 2013: (a,b) magnetic and electric field spectrograms; (c) the ratio of parallel and perpendicular electron fluxes at different energies (see text for details); (d) the average amplitude of the electric field fluctuations (averaged for < 300 Hz fluctuations); (e,f) waveforms of magnetic and electric fields captured during the period of enhanced electric field fluctuations; (g) one of electric field spikes presented in panel (f); (h,i) electron pitch angle distributions observed during weak and intense electric field fluctuations; (j) field-aligned phase space densities corresponding (h) and (i).

Fig. 2: Observations of field-aligned electron PADs conjugated with observation of TDSs on November 1, 2012. The data format is the same as for Fig. 1.